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Absolute Error : The absolute error is used to denote the actual value of a quantity less its rounded value if x and x^* are respectively the rounded and actual values of a quantity, then absolute error is defined by $AE = |x - x^*|$

Accuracy : The Extent of the closeness between the actual value and estimated value is known as accuracy. Suppose you have taken readings like 2.1234, 2.1236 and 2.1238 and 2.45, 2.52, 2.63. Now if the actual root is 2.65 then the second values are more accurate and not precise but first set of values is precise but not accurate as it differs from the actual value.

Algebraic equation : The equation $f(x)=0$ is known as algebraic equation if it is purely a polynomial in x . Like $f(x)=3x^3-3x-4$ are some examples of algebraic equations and if the variable is changed to y or x or any one then under the same conditions it will be algebraic.

Bisection method : It is a bracketing method which is used to locate the root of an equation and it makes use of the intermediate value property to locate the interval in which the root lies. The formula which is used is $(a+b)/2$ where a and b are points such that $f(a)f(b) < 0$.

Bracketing Method : The iterative methods which require two initial approximations for its first iteration are known as bracketing methods. Bisection method is the example of the bracketing method as it requires an interval for the approximation of the root.

LU Method : This method is used to solve the system of equations by decomposing the system into two matrices L and U where L is a lower triangular matrix and U is an upper triangular matrix. In U all the elements in the main diagonal are 1.

Descartes rule of signs : The number of positive roots of an algebraic equation $f(x)=0$ with real coefficients cannot exceed the number of changes in the sign of the coefficients in the polynomial $f(x)=0$, similarly the number of negative roots of $f(x)=0$ cannot exceed the number of changes in the sign of the coefficients of $f(-x)=0$.

Direct methods : These are the methods which do not need the knowledge of the initial approximation and are known as direct methods.

Gauss Elimination Method : It is a direct method which is used to solve a system of equations.

Gauss seidel iterative method : It is an iterative method in which an initial approximation is given. First of all the system should be checked either it is diagonally dominant or not. If it is not then it is made diagonally dominant. Secondly the first variable is calculated in terms of other variables from the first equation and the second variable from the second equation and so on. The previous value of the variable is replaced by the new value instantly as it is obtained. This is the difference between the Gauss-Seidel and Jacobi iterative methods.

Graeffe's root squaring method : This method is used to find all the roots of the polynomial equation.

Intermediate value property : If for an equation $f(x)=0$ for two values a and b we have such that $f(a)f(b) < 0$ then there must exist a root between a and b in the interval $[a, b]$.

Inverse of a matrix : The matrix B is said to be the inverse of a matrix A if the product of A and B is the identity matrix I .

Iterative methods : Iterative methods are those type of methods which always require an initial

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approximation to start an iteration

Jacobie's iterative method :

It is an iterative method in which an initial approximation is given. First of all system should be checked either it is diagonally dominant or not if it is not then it is made diagonally dominant. Secondly the first variable is calculated in terms of other variables from first equation and Second variable from second equation and so on after first iteration in the second iteration all the variables are replaced by the previous one.

Muller's Method :

In Muller's method $f(x)=0$ is approximated by a second degree polynomial, that is by quadratic equation that fits through three points in the vicinity of a root. Then roots of this quadratic equation are then approximated to the roots of equation $f(x)=0$

Newton Raphson Method. :

It is an open method which is used to locate a root of the equation, it needs only one initial approximation for it's first iteration. $x_{n+1}=x_n-(f(x_n)/f'(x_n))$

Non singular matrix :

A matrix is said to be non singular if the determinant of the matrix is non zero. $|A|$ is not equal to zero and the inverse of non singular exists.

Open methods :

The methods which require only one initial approximation to start the first iteration, for example the Newton's Raphson method is known as the open method as it requires only one initial approximation.

Pivoting :

If any of the pivot elements in gauss elimination become zero then this method fails so to Avoid such type of situation equation are rearranged to get rid of zero pivot element, this procedure is known as pivoting.

Precision :

The extent of closeness of different measurement taken to estimate a certain value. Suppose you have done different iterations to measure the root of an equation and take different values as 2.1234, 2.1236, and 2.1238 these all the values are very close to each other so these are very precise.

Regula –Falsi method :

It is also an iterative method and is a bracketing method and use intermediate value property to get it's initial guess. The formula used for this is $x_{n+1}=x_n-(x_n-x_{n-1}/f(x_n)-f(x_{n-1}))$

Relative Error :

It is the ratio of the absolute error to the actual value of the quantity. Thus $RE=AE/AE^*$

Relaxation method :

It is also an iterative method and in this method you solve the system of equation by making the greatest residual to zero.

Root :

If you have an equation $f(x)=0$ then the no a is said to be the root of the equation if $f(a)=0$ Suppose you have an equation $f(x)=x^2-4$ the 2 is a root of the equation as $f(2)=4-4=0$

Secant Method :

The secant method is also an open method and it takes two initial values for it's first approximation, the formula used for this is known as $x_{n+1}=\{x_n-1f(x_n)-x_n f(x_{n-1})\}/\{f(x_n)-f(x_{n-1})\}$

Significant digits :

A significant digit in an approximate no is a digit, which gives reliable information about the size of the number. In other words a significant digit is used to express accuracy, that Is how many digits in the no have meaning.

Singular matrix :

A matrix is said to be a singular matrix if the determinant of the matrix is zero $|A|=0$, the inverse of the singular matrix do not exist.

Transcendental equation :

An equation $f(x)=0$ is said to be transcendental equation if it contains trigonometric, logarithmic and exponential functions

Truncation Error :

It is defined as the replacement of one series by another series with fewer terms.

Question:

What is Bracketing method?

Answer:

Methods such as bisection method and the false position method of finding roots of a nonlinear equation $f(x) = 0$ require bracketing of the root by two guesses. Such methods are called bracketing methods. These methods are always convergent since they are based on reducing the interval between the two guesses to zero.

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SHORT QUESTION ANSWERS

Question:

What is an Open method?

Answer:

In the Newton-Raphson method, the root is not bracketed. Only one initial guess of the root is used to get the iterative process started to find the root of an equation. Hence, the method falls in the category of open methods.

Question:

Explain Muller's method briefly.

Answer:

In Muller's method, $f(x) = 0$ is approximated by a second degree polynomial; that is by an equation that fits through three points in the vicinity of a root. The roots of this quadratic equation are then approximated to the roots of the equation $f(x) = 0$. This method is iterative in nature and does not require the evaluation of derivatives as in Newton-Raphson method. This method is used to determine both real and complex roots of $f(x) = 0$.

Question:

Explain the difference between the linear and non-linear equations.

Answer:

Linear Equation An algebraic equation is said to be linear in which each term is either a constant or the product of a constant and the first power of a single variable. One or more variables are involved in the linear equations. e.g. $x+3y+z=0$ $2x-y+4z=7$ etc. **Non-Linear Equation** An algebraic equation is said to be Non-Linear equation if it is not linear. Equations involving the power of the variable greater than one, or higher, transcendental, logarithmic and trigonometric equations etc lie in the category of Non-Linear equations. e.g. $x^2+5x+3=0$ $\sin x+3y+9=0$ $x \log x-7x+4y=2$ etc.

Question:

Explain which value is to be chosen as X_0 in N-R method.

Answer:

If, for a given function, $f(a)*f(b)<0$, then any value between a and b inclusive can be chosen as X_0 .

Question:

Define iterative method of solving linear equations with two examples.

Answer:

Under iterative methods, the initial approximate solution is assumed to be known and the process converges towards the exact solution in an iterative way. We consider Jacobi, Gauss-Seidel and Successive Over-Relaxation methods under iterative methods.

Question:

Define Pivoting.

Answer:

The Gaussian elimination method fails if any one of the pivot elements becomes zero. In such a situation, we rewrite the equations in a different order to avoid zero pivots. Changing the order of equations is called pivoting.

Question:

Write the two steps of solving the linear equations using Gaussian Elimination method.

Answer:

In this method, the solution to the system of equations is obtained in two stages. i) the system of equations is reduced to an equivalent upper triangular form using elementary transformations. ii) the upper triangular system is solved using back substitution procedure.

Question:

Describe Gauss-Jordan elimination method briefly

Answer:

This method is a variation of Gaussian elimination method. In this method, the elements below the diagonal are simultaneously made zero. That is a given system is reduced to diagonal form using elementary transformations. Then the solution of the resulting diagonal system is obtained.

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is obtained. Sometimes, we normalize the pivot row with respect to the pivot element, elimination. Partial pivoting is also used whenever the pivot element becomes zero.

Question:

Describe briefly Crout's reduction method.

Answer:

Here the coefficient matrix $[A]$ of the system of equations is decomposed into the product of two matrices $[L]$ and $[U]$, where $[L]$ is a lower-triangular matrix and $[U]$ is an upper-triangular matrix with 1's on its main diagonal.

Question:

Describe briefly the Jacobi's method of solving linear equations.

Answer:

This is an iterative method, where initial approximate solution to a given system of equations is assumed and is improved towards the exact solution in an iterative way.

Question:

What is the difference between Jacobi's method and Gauss Seidel method?

Answer:

The difference between Jacobi's method and Gauss Seidel method is that in Jacobi's method the approximations calculated are used in the next iteration for the next approximation but in the Gauss-Seidel method the new approximation calculated is instantly replaced by the previous one.

Question:

What is the basic idea of Relaxation method?

Answer:

We can improve the solution vector successively by reducing the largest residual to zero in each iteration. This is the basic idea of relaxation method.

Question:

How the fast convergence in the relaxation method is achieved?

Answer:

To achieve the fast convergence of the procedure, we take all terms to one side and divide the equations so that the largest negative coefficients in the equations appear on the diagonal.

Question:

Which matrix will have an inverse?

Answer:

Every square non-singular matrix will have an inverse.

Question:

What are the popular methods available for finding the inverse of a matrix?

Answer:

Gauss elimination and Gauss-Jordan methods are popular among many methods available for finding the inverse of a matrix.

Question:

Explain Gaussian Elimination Method for finding the inverse of a matrix.

Answer:

In this method, if A is a given matrix, for which we have to find the inverse; at first, we form an augmented matrix, whose order is same as that of A , adjacent to A which we call an augmented matrix. Then the inverse of A is computed in two stages. In the first stage, A is converted into upper triangular form, using Gaussian elimination method. In the second stage, the above upper triangular matrix is reduced to an identity matrix by row transformations. All these operations are performed on the adjacently placed identity matrix. Finally, when A is transformed into an identity matrix, the adjacent matrix gives the inverse of A . In order to increase the accuracy of the result, we employ partial pivoting.

Question:

What are the steps for finding the largest eigen value by power method.

Answer:

Procedure Step 1: Choose the initial vector such that the largest element is unity. Step 2: The normalized vector is pre-multiplied by the matrix $[A]$. Step 3: The resultant vector is again normalized.

Question:

What is the method for finding the eigen value of the least magnitude of the matrix $[A]$?

Answer:

For finding the eigen value of the least magnitude of the matrix $[A]$, we have to

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apply power method to the inverse of [A].

Question:

What is interpolation?

Answer:

The process of estimating the value of y, for any intermediate value of x, is called interpolation.

Question:

What is extrapolation?

Answer:

The method of computing the value of y, for a given value of x, lying outside the table of x is known as extrapolation.

Question:

What happens when shift operator E operates on the function.

Answer:

When shift operator E operates on the function it results in the next value of the function.

Question:

What is the basic condition for the data to apply Newton's interpolation methods?

Answer:

To apply Newton's interpolation methods, data should be equally spaced.

Question:

When is the Newton's forward difference interpolation formula used?

Answer:

Newton's forward difference interpolation formula is mainly used for interpolating the values near the beginning of a set of tabular values and for extrapolating values of y, a short distance forward from y_0 .

Question:

When is the Newton's backward difference interpolation formula used?

Answer:

Newton's backward difference interpolation formula is mainly used for interpolating the values near the end of a set of tabular values and for extrapolating values of y, a short distance backward from y_0 .

Question:

When the Newton's backward difference interpolation formula is used?

Answer:

For interpolating the value of the function $y = f(x)$ near the end of table of values, and for extrapolating value of the function a short distance forward from y_n , Newton's backward difference interpolation formula is used.

Question:

What is the formula for finding the value of p in Newton's forward difference interpolation formula?

Answer:

$P = (x - x_0)/h$

Question:

What is the formula for finding the value of p in Newton's backward difference interpolation formula?

Answer:

$P = (x - x_n)/h$

Question:

If the values of the independent variable are not equally spaced then which formula should be used for interpolation?

Answer:

If the values of the independent variable are not given at equidistant intervals, then the divided difference interpolation formula should be used.

Question:

To use Newton's divided difference interpolation formula, what should the values of independent variable be?

Answer:

To use Newton's divided difference interpolation formula, the values of independent variable should not be equally spaced.

Question:

Which difference formula is symmetric function of its arguments?

Answer:

Divided difference formula is symmetric function of its arguments.

Question:

Is the interpolating polynomial found by Lagrange's and Newton's divided difference formulae is same?

Answer:

Yes. The interpolating polynomial found by Lagrange's and Newton's divided difference formulae is same.

MTH603 FAQ+ Short Questions Answers

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formulae is one and the same.

Question: Which formula involves less number of arithmetic operations? Newton or Lagrange's?

Answer: Newton's formula involves less number of arithmetic operations than that of Lagrange's.

Question: When do we need Numerical Methods for differentiation and integration?

Answer: If the function is known and simple, we can easily obtain its derivative (s) or can evaluate definite integral. However, if we do not know the function as such or the function is given in a tabular form at a set of points x_0, x_1, \dots, x_n , we use only numerical methods for differentiation or integration of the given function.

Question: If the value of the independent variable at which the derivative is to be found appears at the beginning of the table of values, then which formula should be used?

Answer: If the value of the independent variable at which the derivative is to be found appears at the beginning of the table, it is appropriate to use formulae based on forward differences to find derivatives.

Question: If the value of the independent variable at which the derivative is to be found occurs at the end of the table of values, then which formula should be used?

Answer: If the value of the independent variable at which the derivative is to be found occurs at the end of the table of values, it is appropriate to use formulae based on backward differences to find derivatives.

Question: Why do we need to use RICHARDSON'S EXTRAPOLATION METHOD?

Answer: To improve the accuracy of the derivative of a function, which is computed by starting with an arbitrarily selected value of h , Richardson's extrapolation method is often employed.

Question: To apply Simpson's 1/3 rule, what should the number of intervals be?

Answer: To apply Simpson's 1/3 rule, the number of intervals must be even.

Question: To apply Simpson's 3/8 rule, what should the number of intervals be?

Answer: To apply Simpson's 3/8 rule, the number of intervals must be multiple of 3.

Question: What is the order of global error in Simpson's 1/3 rule?

Answer: The global error in Simpson's 1/3 rule is of the order of $O(h^4)$.

Question: Is the order of global error in Simpson's 1/3 rule equal to the order of global error in Simpson's 3/8 rule?

Answer: Yes. The order of global error in Simpson's 1/3 rule is equal to the order of global error in Simpson's 3/8 rule.

Question: What is the order of global error in Trapezoidal rule?

Answer: The global error in Trapezoidal rule is of the order of $O(h^2)$.

Question: What is the formula for finding the width of the interval?

Answer: Width of the interval, h , is found by the formula $h=(b-a)/n$

Question: What type of region does the double integration give?

Answer: Double integration gives the area of the rectangular region.

Question: Compare the accuracy of Romberg's integration method to trapezoidal and Simpson's rule.

Answer: Romberg's integration method is more accurate than trapezoidal and Simpson's rule.

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require any type of initial approximation.

Question:

What is Iterative method of solving equations?

Answer:

These methods require an initial approximation to start. Bisection method, Newton raphson method, secant method, jacobi method are all examples of iterative methods

Question:

If an equation is a transcendental, then in which mode the calculations should be done?

Answer:

All the calculations in the transcendental equations should be done in the radian mode

Question:

What is the convergence criterion in method of iteration?

Answer:

If x be a root of $f(x) = 0$ which is equivalent to I be any interval containing the point $x = a$ converge to the root provided that the initial approximation is chosen in I

Question:

When we stop doing iterations when TOL is given?

Answer:

Here if TOL is given then we can simply find the value of TOL by subtracting both the consecutive roots and write it in the exponential notation if the required TOL is obtained

Question:

What is a transcendental equation?

Answer:

An equation is said to be a transcendental equation if it has trigonometric, exponential, logarithmic function or combination of all these functions.

Question:

How the value of h is calculated in interpolation?

Answer:

There are two types of data in the interpolation one is equally spaced and other is unequally spaced data we need to calculate the value of h that is calculated by subtracting consecutive values and taking their absolute value.

Question:

What is an algebraic equation?

Answer:

An algebraic equation is an equation which is purely polynomial in any variable. Supposed $x^2+3x+2=0$, $x^4+3x^2=0$, $y^3+6y^2=0$ all are algebraic equations as these are polynomial in x and y variable.

Question:

What is Descartes rule of signs?

Answer:

The number of positive roots of an algebraic equation $f(x) = 0$ can not exceed the no of signs. Similarly the no of negative roots of an algebraic equation can not exceed the no of changes in sign of equation $f(-x) = 0$.

Question:

What are direct methods?

Answer:

The numerical methods which need no information about the initial approximation are called direct methods like Graeffe's root squaring method.

Question:

What is meant by iterative methods?

Answer:

The methods which need one or more iterations are known as iterative methods like bisection method, Newton raphson method, and many other methods.

Question:

What is graphically meant by the root of the equation?

Answer:

If the graph of a function $f(x) = 0$ cuts the x -axis at a point a then a is known as the root of the equation.

Question:

Q. What is the difference between open and bracketing method?

Answer:

In open methods we need only one initial approximation of the root that may be any where

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if it is not very close then we have to perform more iteration and the example of open Newton Raphson method. In bracketing method we bracket the root and find that interval where the root lies means we need two initial approximations for the root finding. Bisection method is an example of the bracketing method.

Question: Condition for the existence of solution of the system of equations.

Answer: If the $|A|$ is not equal to zero then the system will have a unique solution if $|A|=0$ then it will have no solution

Question: Should the system be diagonally dominant for Gauss elimination method?

Answer: The system of equations need not to be diagonally dominant for Gauss elimination method or Gauss Jordan method for both the direct methods it is not necessary for the system to be diagonally dominant. It should be diagonally dominant for iterative methods like Jacobi and Gauss-Seidel method.

Question: What is meant by diagonally dominant system?

Answer: A system $a_1x+b_1y+c_1z=d_1$, $a_2x+b_2y+c_2z=d_2$, $a_3x+b_3y+c_3z=d_3$ is said to be diagonally dominant if the following condition holds.

$|a_1| \geq (|b_1|+|c_1|)$ $|a_2| \geq (|b_2|+|c_2|)$ $|a_3| \geq (|b_3|+|c_3|)$

Question: State the sufficient condition for the convergence of the system of equations by iterative methods.

Answer: A sufficient condition for convergence of iterative solution to exact solution is

$|a_1| \geq (|b_1|+|c_1|)$ $|a_2| \geq (|b_2|+|c_2|)$ $|a_3| \geq (|b_3|+|c_3|)$ For the system $a_1x+b_1y+c_1z=d_1$, $a_2x+b_2y+c_2z=d_2$, $a_3x+b_3y+c_3z=d_3$. Similarly for the system with more variables we can also construct the same condition.

Question: The calculation for numerical analysis should be done in degree or radians.

Answer: All the calculation for numerical analysis should be done in radians not in degrees. Set your calculator in radians mode and suppose the value of $\pi=3.14$.

Question: How we can identify that Newton forward or backward interpolation formula is to be used.

Answer: If the value at which we have to interpolate is in the start of the table then we will use Newton's forward interpolation formula. If it is at the end of the table then we will use Newton's backward interpolation formula.

Question: What is meant precision and accuracy?

Answer: Precision and accuracy are two terms which are used in numerical calculations. Precision means that how the values in different iterations agree to each other or how close are the values in successive iterations. For example you have performed 3 different iterations and the result of all the iterations are 1.32514, 1.32516, 1.32518. These three values are very precise because these values agree with each other. Accuracy means the closeness to the actual value. For example, if you have calculated an answer after some iteration and the answer is 2.718245 and the actual answer is 2.718254, then the answer calculated is very accurate but if this answer is 2.71824 then it is not accurate.

Question: What is the condition that a root will lie in an interval.

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decimal and discard all the remaining terms.

Explanation $(1/3 - 3/11) + 3/20 = (0.333333... - 0.27272727...) + 0.15 = (0.333 - 0.272) + 0.15$

This is the three digit chopping.

Question:

[When the forward and backward interpolation formulae are used?](#)

Answer:

In interpolation if we have at the start then we use the forward difference formula and calculate p is $x-x_0/h$. If the value of x lies at the end then we use Newton's backward formula to calculate the value of p is $x-x_n/h$. Now I come to your question as in this x lies at the end so 6 will be used as the x_n . This procedure has been followed by the teacher in the lectures. But some authors also use another technique that is if you calculate the value of p that is negative then the origin is shifted to that value for which the value of p becomes 0. And then according to that origin the values of differences are used and you need not follow the forward procedure.

Question:

[What is forward and backward difference operator and the construction of their table.](#)

Answer:

For forward $Df_r = f_{r+1} - f_r$ $Df_0 = f_1 - f_0$ In terms of y $Dy_{r+1} = y_{r+1} - y_r$ D stands for the forward difference operator For backward $Df_r = f_r - f_{r-1}$ $Df_1 = f_1 - f_0$ In terms of y $Dy_1 = y_1 - y_0$ D stands for backwards operator Now the construction of the difference table is based on 1st forward 2nd forward 3rd forward
 x_1 Y_1 $Y_2 - Y_1 = Dy_0$ x_2 Y_2 $Y_3 - Y_2 = Dy_1$ x_3 Y_3 $Y_4 - Y_3 = Dy_2$ x_4 Y_4 Now consider the construction of table for the backward table

X Y 1st forward 2nd forward 3rd forward

x_1 Y_1 $Y_2 - Y_1 = Dy_1$ x_2 Y_2 $Y_3 - Y_2 = Dy_2$ x_3 Y_3 $Y_4 - Y_3 = Dy_3$ x_4 Y_4 D

Dear student this is the main difference in the construction of the forward and backwards difference table when you proceed for forward difference table you get in the first difference the value Dy_0 but in the construction of backwards difference table in the first difference you get Dy_1 and in the second difference in the forward difference table you get $D^2 y_0$ and in the backward difference table the first value in the second difference is $D^2 y_1$. I think so you have made it clear.

Question:

[What is Jacobi's method?](#)

Answer:

Jacobi's Method It is an iterative method and in this method we first of all check either the system is diagonally dominant and, if the system is diagonally dominant then we will calculate the value of first variable from first equation in the form of other variables and from the second equation the value of second variable in the form of other variables and so on. We are given with the initial approximations and these approximations are used in the first iteration to get the first approximation of all the variables. The approximations calculated in the first iteration are used in the second iteration to calculate the second approximations and so on.

Question:

[what is Simpson's 3/8th rule.](#)

Answer:

The general formula for Simpson's 3/8th rule is

$$\frac{3h}{8}[f_0 + 3(f_1 + f_2) + 2f_3 + (3f_4 + f_5) + 2f_6 + \dots + 3(f_{n-2} + f_{n-1}) + f_n]$$

Now if we have to calculate the integral by using this rule then we can simply proceed just write first and last value and distribute all the remaining values with prefix 3 and 2 Like you have f_0, f_1, f_2, f_3, f_4 Then the integral can be calculated as $\frac{3h}{8}[f_0 + f_4 + 3(f_1 + f_2) + 2f_4]$ If we have values like $f_0, f_1, f_2, f_3, f_4, f_5$ Then integral can be calculated as $\frac{3h}{8}[f_0 + 3(f_1 + f_2) + 2f_3 + 3f_4 + f_5]$ Similarly proceeding in this fashion we can calculate the integral in this fashion

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Question: [what is classic runge-kutta method](#)

Answer: The fourth order Runge-Kutta method is known as the classic formula of classic Runge-Kutta method.

$$y_{n+1} = y_n + \frac{1}{6}(k_1 + 2k_2 + 2k_3 + k_4)$$

Where $k_1 = hf(x_n, y_n)$ $k_2 = hf(x_n + h/2, y_n + k_1/2)$
 $k_3 = hf(x_n + h/2, y_n + k_2/2)$ $k_4 = hf(x_n + h, y_n + k_3)$

Question: [What is meant by TOL?](#)

Answer: The TOL means the extent of accuracy which is needed for the solution. If you need the solution to two places of decimal then the TOL will be 10^{-2} . Similarly the 10^{-3} means that the solution is needed to three places of decimal. Suppose you have the root from last iteration 0.8324525. If we subtract both and consider absolute value of the difference 0.0000009, it can be written as 0.09×10^{-5} so the TOL in this case is 10^{-5} . Similarly if we have been given a problem where you have to find the TOL 10^{-2} you will check in the same way. In the given equation you solve the equation by any method and will consider some specific TOL and try to go to that TOL. Some time no TOL is provided and you are asked to perform to some specific no of iterations.

Question: [what is meant by uniqueness of LU method.](#)

Answer: An invertible (whose inverse exists) matrix can have LU factorization if and only if all its principal minors (the determinant of a smaller matrix in a matrix) are non zero. The factorization is unique if we require that the diagonal of L or U must have 1's. The matrix has a unique LDU factorization under these conditions. If the matrix is singular (inverse does not exist) then an LU factorization may still exist. For a square matrix of rank k (the rank of a matrix in a field is the maximal no of rows or columns), it has an LU factorization if the first k principal minors are non zero. These are the conditions for the uniqueness of the LU decomposition.

Question: [how the value of h is calculated from equally spaced data.](#)

Answer: Consider the following data:
x y
1 1.6543
2 1.6984
3 2.4546
4 2.9732
5 3.2564
6 3.8765
Here for $h = 2 - 1 = 3 - 2 = 1$
x y
0.1 1.6543
0.2 1.6984
0.3 2.4546
0.4 2.9732
0.5 3.2564
0.6 3.8765
Here for the calculation of $h = 0.2 - 0.1 = 0.3 - 0.2 = 0.1$ I think so that you may be able to understand.