

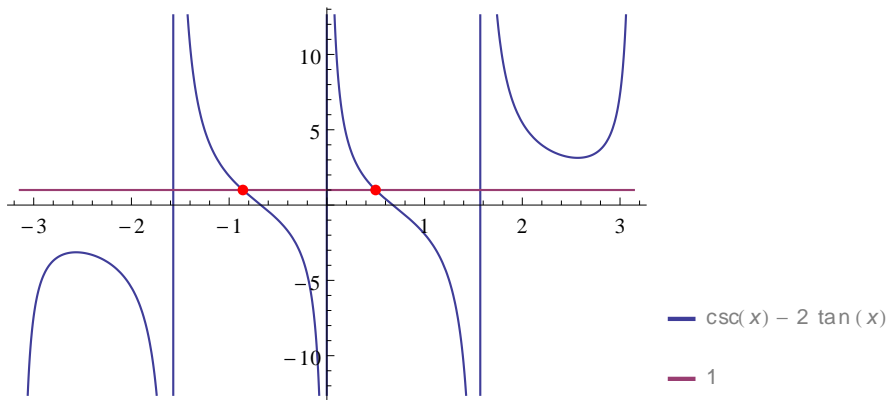
$$\csc(x) - 2 \tan(x) = 1$$



Input:

$$\csc(x) - 2 \tan(x) = 1$$

Plot:



Alternate forms:

$$\csc(x) = 2 \tan(x) + 1$$

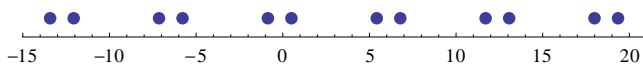
Alternate form assuming  $x$  is real:

$$-\frac{2 \sin(x)}{\cos(2x) - 1} - \frac{2 \sin(2x)}{\cos(2x) + 1} = 1$$

Solutions:

$$x \approx 2. (3.14159 n - 0.429693), \quad n \in \mathbb{Z}$$

Number line:



Real solutions:

$$x = -\tan^{-1} \left( \frac{1}{4} \left( 1 - \frac{66}{25} \sqrt{\frac{3}{92 + 5 \sqrt{6616 - 24 \sqrt{273}} + 10 \sqrt{827 + 3 \sqrt{273}}}} \right) \right) +$$

$$\begin{aligned}
 & \frac{\sqrt[3]{6616 - 24\sqrt{273}} \sqrt{92 + 5\sqrt[3]{6616 - 24\sqrt{273}} + 10\sqrt[3]{827 + 3\sqrt{273}}} + \sqrt[3]{827 + 3\sqrt{273}} \sqrt{92 + 5\sqrt[3]{6616 - 24\sqrt{273}} + 10\sqrt[3]{827 + 3\sqrt{273}}}}{40\sqrt{3}} + \\
 & \frac{\sqrt[3]{827 + 3\sqrt{273}} \sqrt{92 + 5\sqrt[3]{6616 - 24\sqrt{273}} + 10\sqrt[3]{827 + 3\sqrt{273}}} - \sqrt[3]{6616 - 24\sqrt{273}} \sqrt{92 + 5\sqrt[3]{6616 - 24\sqrt{273}} + 10\sqrt[3]{827 + 3\sqrt{273}}}}{20\sqrt{3}} - \\
 & \frac{\left(92 + 5\sqrt[3]{6616 - 24\sqrt{273}} + 10\sqrt[3]{827 + 3\sqrt{273}}\right)^{3/2}}{600\sqrt{3}} - \\
 & \frac{7}{50} \sqrt{3 \left(92 + 5\sqrt[3]{6616 - 24\sqrt{273}} + 10\sqrt[3]{827 + 3\sqrt{273}}\right)} + \\
 & 7 / \left( 5 \sqrt{ \left( 3 / \left( \left( 92 + 5\sqrt[3]{6616 - 24\sqrt{273}} + 10\sqrt[3]{827 + 3\sqrt{273}} \right) \right. \right. \right. \\
 & \left. \left. \left. \left( \frac{184}{75} - \frac{1}{15} \sqrt[3]{6616 - 24\sqrt{273}} - \frac{2}{15} \sqrt[3]{827 + 3\sqrt{273}} + \frac{24}{25} \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \sqrt{\frac{3}{92 + 5\sqrt[3]{6616 - 24\sqrt{273}} + 10\sqrt[3]{827 + 3\sqrt{273}}}} \right) \right) \right) \right) - \\
 & \frac{1}{5} \sqrt{ \left( \frac{184}{75} - \frac{1}{15} \sqrt[3]{6616 - 24\sqrt{273}} - \frac{2}{15} \sqrt[3]{827 + 3\sqrt{273}} + \right. \\
 & \left. \frac{24}{25} \sqrt{\frac{3}{92 + 5\sqrt[3]{6616 - 24\sqrt{273}} + 10\sqrt[3]{827 + 3\sqrt{273}}}} \right) } +
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{8} \sqrt[3]{6616 - 24\sqrt{273}} \sqrt{\left( \frac{184}{75} - \frac{1}{15} \sqrt[3]{6616 - 24\sqrt{273}} - \right.} \\
 & \quad \left. \frac{2}{15} \sqrt[3]{827 + 3\sqrt{273}} + \right.} \\
 & \quad \left. \frac{24}{25} \sqrt{\frac{3}{92 + 5\sqrt[3]{6616 - 24\sqrt{273}} + 10\sqrt[3]{827 + 3\sqrt{273}}}} \right) +} \\
 & \frac{1}{4} \sqrt[3]{827 + 3\sqrt{273}} \sqrt{\left( \frac{184}{75} - \frac{1}{15} \sqrt[3]{6616 - 24\sqrt{273}} - \frac{2}{15} \sqrt[3]{827 + 3\sqrt{273}} + \right.} \\
 & \quad \left. \frac{24}{25} \sqrt{\frac{3}{92 + 5\sqrt[3]{6616 - 24\sqrt{273}} + 10\sqrt[3]{827 + 3\sqrt{273}}}} \right) +} \\
 & \frac{5}{8} \left( \frac{184}{75} - \frac{1}{15} \sqrt[3]{6616 - 24\sqrt{273}} - \frac{2}{15} \sqrt[3]{827 + 3\sqrt{273}} + \right. \\
 & \quad \left. \frac{24}{25} \sqrt{\frac{3}{92 + 5\sqrt[3]{6616 - 24\sqrt{273}} + 10\sqrt[3]{827 + 3\sqrt{273}}}} \right)^{3/2} -} \\
 & \frac{1}{10} \sqrt{\left( 3 \left( 92 + 5\sqrt[3]{6616 - 24\sqrt{273}} + 10\sqrt[3]{827 + 3\sqrt{273}} \right) \right.} \\
 & \quad \left. \left( \frac{184}{75} - \frac{1}{15} \sqrt[3]{6616 - 24\sqrt{273}} - \frac{2}{15} \sqrt[3]{827 + 3\sqrt{273}} + \right. \right.} \\
 & \quad \left. \left. \frac{24}{25} \sqrt{\frac{3}{92 + 5\sqrt[3]{6616 - 24\sqrt{273}} + 10\sqrt[3]{827 + 3\sqrt{273}}}} \right) \right) \right) \approx
 \end{aligned}$$

-0.859387

Wolfram|Alpha:  $\csc(x) - 2\tan(x) = 1$